

Lecture 15 QAM Transmitters

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Analog/RF Front Ends

- [Announcement](#)
- What does that transmission actually look like on a laptop?
 - Computational platform in the base of the laptop under the keyboard
 - CPUs running at a clock speed of 1.6 to 5 GHz
 - [PCI Express](#) data lines – each serial line transmits 10 bits at a time with an 8-bit data and 2-bit embedded clock for timing synchronization operating at a clock speeds of 1.25, 2.5, 4, 8, or 16 GHz for 1-5 generations, respectively. Each “lane” has a serial line in one direction and a second serial line in the other direction for bi-directional communication. Sixth-generation PCI Express uses 4-PAM signaling.
 - Memory – memory locations are written into using an error correcting code so when the data is read, any bit flips can be detected and corrected
 - [Pixel clock driving the display](#) – from 100 MHz to 1 GHz. High-power clock with high-power harmonics that leak and interfere with wireless transmissions
 - Antennas for Wi-Fi and Bluetooth transmission
 - Placed in the laptop lid to maximize distance from the RF emissions of the computational platform including memory I/O and pixel clock and its harmonics
 - This antenna placement reduces the interference of the Wi-Fi and Bluetooth transmissions on the operation of the computational platform under the keyboard and vice-versa

Review of Previous Lecture

- Matched filter
 - Compensates for additive thermal noise in RF front end
 - Placed in the baseband signal processing in the receiver after demodulation
 - Optimal matched filter impulse response: conjugated time-reversed pulse shape

Matched Filter - Maximize SNR in Receiver

$$h_{opt}(t) = k g^*(T_{sym} - t) \text{ for pulse shape } g(t)$$

any gain $(k \neq 0)$ any integer multiple will do to make $h_{opt}(t)$ causal

$$|H_{opt}(f)| = |k| |G(f)|$$

Baseband BW = $\frac{1}{2} f_{sym} (1 \pm \alpha)$ $G(f)$ is lowpass \rightarrow $H(f)$ is lowpass

raised cosine

- Can be delayed any integer multiple of T_{sym}
- Can have any gain k but $k \neq 0$ in practice ($k=0$ means nothing gets through)
- Baseband bandwidth for raised cosine is between $\frac{1}{2} f_{sym}$ to f_{sym}

- Discrete time
 - L samples per symbol, so delay by L samples rather than T_{sym} in continuous time

Discrete-Time

$$h[m] = k g^*[L-m]$$

m is associated w/
the sampling rate f_s of
the AD converter:

$$f_s = L f_{\text{sym}}$$

$$\frac{1}{T_s} = L \frac{1}{T_{\text{sym}}}$$

$$h_{\text{opt}}[m] = h_{\text{opt}}(t) \Big|_{t=T_s m} = k g^*(T_{\text{sym}} - T_s m)$$

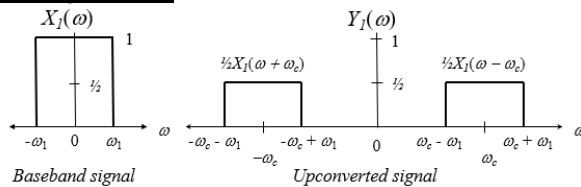
$$T_{\text{sym}} = L T_s : h_{\text{opt}}[m] = \frac{1}{L} g^*(L T_s - m T_s)$$

$$h_{\text{opt}}[m] = k g^*[L-m] \leftarrow \text{flip } g(m), \text{ conjugate, delay to make it causal, scale by } k$$

QAM

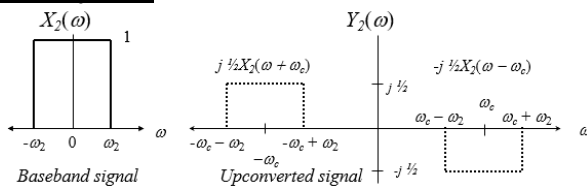
- 2D PAM
- Increase bit rate while using same transmission bandwidth as upconverted PAM
- Essentially 2 M-PAM signals, one modulated with a cosine and the other modulated by a sine and placed in the same transmission band for spectral efficiency
- Because the bit information is transmitted in the amplitude and phase, the QAM receiver more sensitive to phase error than a PAM receiver
- Need to scale by 2 somewhere in the receiver to compensate for loss in modulation

Modulation by cosine



- Modulated signal is real-valued in the frequency domain
- Demodulate using modulation by the cosine and lowpass filtering

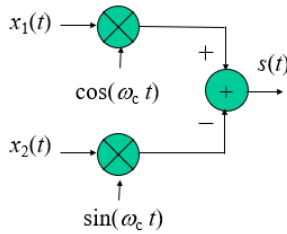
Modulation by sine



- Modulated signal is imaginary-valued in the frequency domain

- Demodulate using modulation by the sine and lowpass filtering

QAM bandwidth efficiency

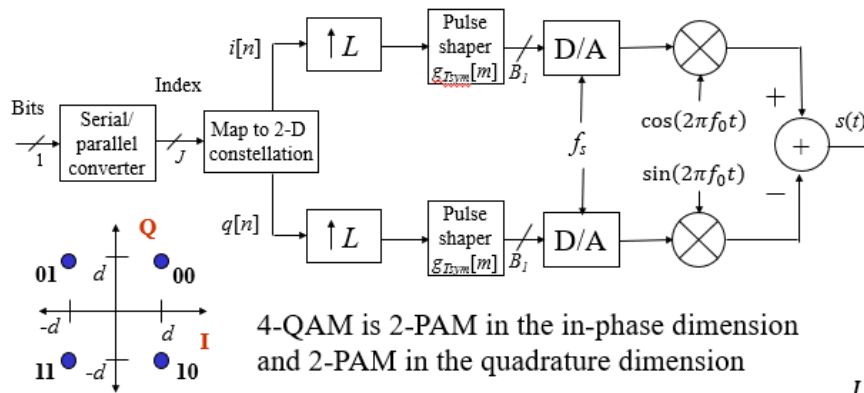


$$S(\omega) = \frac{1}{2}(X_1(\omega + \omega_c) + X_1(\omega - \omega_c)) - j\frac{1}{2}(X_2(\omega + \omega_c) - X_2(\omega - \omega_c))$$

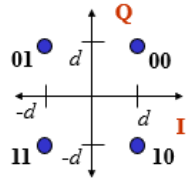
- Cosine modulated signal is orthogonal to sine modulated signal, so can separate through demodulation with cosine and sine, respectively

QAM Architecture 1

- Each component will have a corresponding component in receiver, ie serial/parallel converter in tx and parallel/serial converter in rx



4-level QAM Constellation



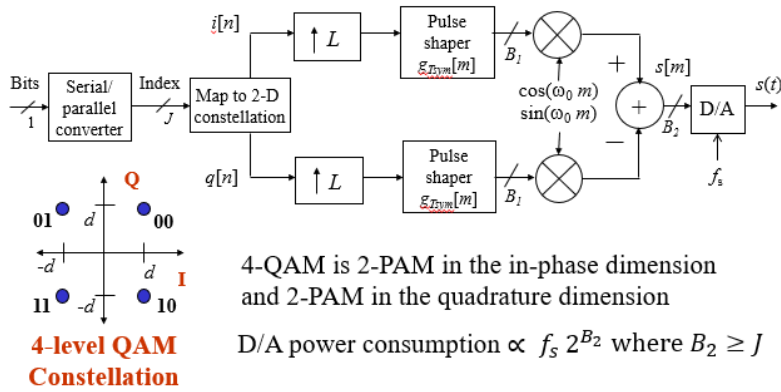
4-QAM is 2-PAM in the in-phase dimension and 2-PAM in the quadrature dimension

D/A power consumption $\propto f_s 2^{B_1}$ where $B_1 \geq \frac{J}{2}$

- 4-QAM constellation will include 2-PAM in the in-phase dimension (horizontal dimension) and 2-PAM in quadrature dimension (vertical dimension)
- Upsample, pulse shape, and D/A converter is the same for I and Q component
- This architecture upconverts analog signal
 - Lower power than placing modulation in software b/c D/A converter power is exponential in the number of bits
- Each D/A converter must handle $\geq J/2$ bits
 - At least as many bits in the I or Q dimension

QAM Architecture 2

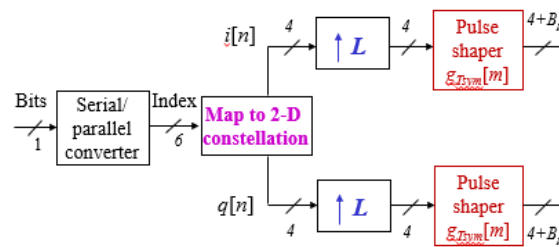
- Done in lab
- Only 1 D/A converter



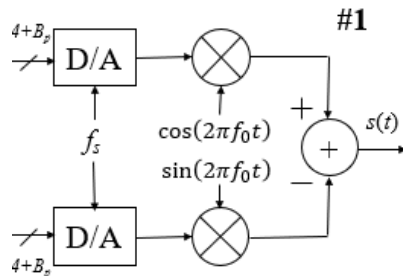
- Need many more bits in D/A converter to accurately represent sine and cosine, so much more power hungry
 - For 4-QAM: 1 bit for I, 1 bit for Q, ~8 bits for sin and cosine

Comparison for 64-QAM

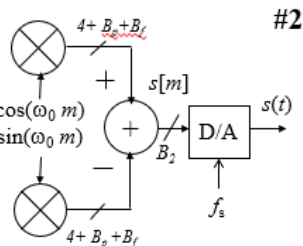
- Same for both architectures:



- i[n] and q[n] are 8-PAM, which need 4 bits each
- Pulse shaper will introduce B_p bits to represent pulse
- Architecture 1:



- $4+B_p$ bits sent to D/A
- Architecture 2:



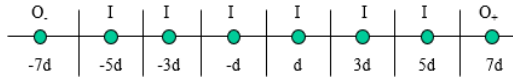
- $4+B_p+B_f$ bits sent to D/A

PAM Performance Analysis

- If we sampled matched filter output at correct time instances without any ISI, received signal only contains tx signal + noise

$$x(nT_{sym}) = s(nT_{sym}) + v(nT_{sym}) \quad v(nT) \sim N(0; \sigma^2/T_{sym})$$

- For 8-PAM :



- Decision error for an inner constellation point – a symbol error can occur in one of two directions. Consider transmitting a symbol amplitude of $-5d$ and receiving a symbol amplitude of $-5d$ plus a random variable following a Gaussian distribution with zero mean and variance $\sigma^2 / \sqrt{T_{sym}}$. An error occurs if the received symbol is less than $-6d$ or greater than $-4d$. The probability of error is calculated by integrating two tails of a normalized Gaussian PDF.

$$P_i(e) = P(|v(nT_{sym})| > d) = 2Q\left(\frac{d}{\sigma\sqrt{T_{sym}}}\right)$$

- Decision error for outer points – a symbol error can occur in only one direction. Consider transmitting a symbol amplitude of $-7d$ and receiving a symbol amplitude of $-7d$ plus a random variable following a Gaussian distribution with zero mean and variance $\sigma^2 / \sqrt{T_{sym}}$. An error occurs if the received symbol is greater than $-6d$. This is similar to the case for 2-PAM– the probability of error is calculated by integrating one tail of a normalized Gaussian PDF.

$$P_{O_-}(e) = P(v(nT_{sym}) > d) = Q\left(\frac{d}{\sigma\sqrt{T_{sym}}}\right)$$

$$P_{O_+}(e) = P(v(nT_{sym}) < -d) = P(v(nT_{sym}) > d) = Q\left(\frac{d}{\sigma\sqrt{T_{sym}}}\right)$$

- Symbol error probability
 - (fraction of inner points) * (decision error for inner points) + (fraction of outer points) * (decision error for outer points)

$$P(e) = \frac{M-2}{M} P_i(e) + \frac{1}{M} P_{O_-}(e) + \frac{1}{M} P_{O_+}(e) = \frac{2(M-1)}{M} Q\left(\frac{d}{\sigma\sqrt{T_{sym}}}\right)$$